A useful item in the Stata toolkit is the returned result. For example, after most estimation commands, parameter estimates are stored in a matrix \texttt{e(b)}. However, these commands do not return the \textit{t} statistics, \textit{p}-values, and confidence intervals for those parameter estimates. The aim here is to show how to recover those statistics by using the results that are returned. Consider the following OLS regression:

\begin{verbatim}
. sysuse auto
(1978 Automobile Data)
. regress price mpg foreign

Source | SS        df       MS          Number of obs = 74
--------+---------------------------------------------
Model   | 180261702   2  90130850.8     F(  2,    71) = 14.07
        | Prob > F    = 0.0000
Residual| 454803695   71  6405685.84   Adj R-squared = 0.2637
        | R-squared   = 0.2838
        | Root MSE    = 2530.9
        |                Total | 635065396   73  8699525.97

price  | Coef.      Std. Err.    t    P>|t|    [95% Conf. Interval]
--------+---------------------------------------------------------------
mpg     | -294.1955   55.69172  -5.28  0.000   -405.2417  -183.1494
foreign | 1767.292   700.1586  2.52   0.014    371.2169   3163.368
_cons   | 11905.42   1158.634 10.28   0.000   9595.164   14215.67

1 \textit{t} statistic

The \textit{t} statistic can be calculated from \( t = \frac{\hat{b} - b}{se} \), where \( \hat{b} \) is the estimated parameter, \( b \) is the parameter value under the null hypothesis, and \( se \) is the standard error. The null hypothesis is usually that the parameter equals zero; thus we have \( t = \frac{b}{se} \). The \textit{t} statistic for one parameter (\texttt{foreign}) can be calculated by

\begin{verbatim}
. di _b[foreign]/_se[foreign]
2.5241336
\end{verbatim}

All the parameter estimates are also returned in the matrix \texttt{e(b)}. A vector of all standard errors is a bit harder to obtain; they are the square roots of the diagonal elements of the matrix \texttt{e(V)}. In Mata that vector can be created by typing \texttt{diagonal(cholesky(diag(V)))}. Continuing the example, a vector of all \textit{t} statistics can be computed within Mata by

\begin{verbatim}
: b = st_matrix("e(b)")
: V = st_matrix("e(V)")
: t = b :/ V
\end{verbatim}

\[ c \odot 2007 \text{StataCorp LP} \]
2 p-value

The p-value can be calculated from \( p = 2 \times (1 - T(df, |t|)) \), where \( T \) is the cumulative distribution function of Student’s t distribution, \( df \) is the residual degrees of freedom, and \(|t|\) is the absolute value of the observed t statistic. The t statistic was calculated before, and the residual degrees of freedom are returned as \( e(df_r) \). The absolute value can be calculated by using the \texttt{abs()} function, and \((1 - T(df, t))\) can be calculated by using the \texttt{ttail(df,t)} function. The calculation is put together as follows:

\[
\text{local } t = \_b[\text{foreign}]/\_se[\text{foreign}]
\]
\[
\text{di } 2\times\text{ttail}(e(df_r),\text{abs('t')})
\]

Using Mata, the vector of all p-values is then

\[
\text{df = st_numscalar("e(df_r)")}
\]
\[
\text{t = b :/ se}
\]
\[
\text{2\times\text{ttail(df, abs(t))}}
\]

3 Confidence interval

The lower and upper bounds of the confidence interval can be calculated as \( \hat{\beta} \pm t_{\alpha/2}se \), where \( t_{\alpha/2} \) is the critical t-value given a significance level \( \alpha/2 \). This critical value can be calculated by using the \texttt{invttail} function. The lower and upper bounds of the 95% confidence interval for the parameter of \texttt{foreign} are thus given by

\[
\text{di } \_b[\text{foreign}] - \text{invttail}(e(df_r),0.025)*\_se[\text{foreign}]
\]

371.2169

\[
\text{di } \_b[\text{foreign}] + \text{invttail}(e(df_r),0.025)*\_se[\text{foreign}]
\]

3163.3676

(Continued on next page)
The vectors of lower and upper bounds for all parameters follow suit in Mata as

\[ b := \text{invttail}(df,0.025) \times \text{se}, \quad b + \text{invttail}(df,0.025) \times \text{se} \]

<table>
<thead>
<tr>
<th></th>
<th>Lower Bound</th>
<th>Upper Bound</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>-405.2416661</td>
<td>-183.1494001</td>
</tr>
<tr>
<td>2</td>
<td>371.2169028</td>
<td>3163.367584</td>
</tr>
<tr>
<td>3</td>
<td>9595.1638</td>
<td>14215.66676</td>
</tr>
</tbody>
</table>

4 Models reporting z statistics

If you are using an estimation command that reports z statistics instead of t statistics, the values become

- \( b[\text{foreign}] / \text{se[foreign]} \) for the z statistic;
- \( 2 \times \text{normal}(-\text{abs}(\text{z})) \) for the p-value (where the minus sign comes from the fact \( \text{normal}() \) starts with the lower tail of the distribution, whereas \( \text{ttail}() \) starts with the upper tail);
- \( b[\text{foreign}] - \text{invnormal}(0.975) \times \text{se[foreign]} \) for the lower bound of the 95% confidence interval, and \( b[\text{foreign}] + \text{invnormal}(0.975) \times \text{se[foreign]} \) for the upper bound (.975 is used instead of .025 for the same kind of reason).

5 Further comments

Often it is unnecessary to do these calculations. In particular, if you are interested in creating custom tables of regression-like output the \texttt{estimates table} command or the tools developed by Jann (2005, 2007) are much more convenient. Similarly, if the aim is to create graphs of regression output, take a good look at the tools developed by Newson (2003) before attempting to use the methods described here. This tip is for situations in which no such command does what you want.

References

